

# **PROBIT MODELS FOR GROUPED-DATA MIGRATION FLOWS: A THEORETICAL NOTE**

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- Conclusions



# I. MOTIVATION

- Interested in the formulation of migration models.
- Migration modeling has been applied to both, micro and macro-levels (*Aleshkovski and Iontsev 2006*):
  - **Micro approach** focuses on the migration behavior of individuals or households based on disaggregated data usually delivered by surveys. They are **costly to collect or inaccessible**. Tool: **Discrete choice models**.
  - **Macro approach** studies the patterns of migration of certain social groups within a given territory. Choice data is aggregated across groups of individuals in the form of counts or shares. **Easier to obtain**. Tool: **Gravity or interaction models**.
- Our database follows a **macro approach** =  
We propose a **PROBIT CHOICE MODEL** but for **GROUPED-DATA** flows, due to some important specification problems of the standard spatial interaction models of flows (*LeSage and Fischer 2010*).



## II. GPROBIT: AN ALTERNATIVE

### II.1. Specification

GProbit = Probit choice model for grouped-data flows.

Theoretical foundation: Random utility theory for aggregations of decisions (probabilities) made by individuals who share a similar characteristic; e.g. living in a same region.

Individual:

$$P(y = 1) = P(y^* \geq 0) = P(U_{od} \geq U_{oo})$$

$$y^* = U_{od} - U_{oo} = x'\theta + u$$



Adding up the independent probabilities for all the individuals who move from o to d.

$$P_{od} = \frac{M_{od}}{R_o} \xrightarrow{\text{Each of the group components} \rightarrow \infty} P_{od} = \pi_{od} + u_{od}$$

$R_o = M_{od} + M_{oo}$   
 $M_{oo}$  = 'stayers' + intra-flows

$\pi_{od} = F(x'_{od}\beta)$   
Theoretical proportion

Share, proportion (relative frequency) of people who migrate from o to d during a certain period ( $M_{od}$ ) over the total resident population living in o 'at risk' of migrating during this same period ( $R_o$ ).

'Meaningful estimates of interaction probabilities between OD pairs' (Sen and Smith 1993)



## II. GPROBIT: AN ALTERNATIVE

### II.1. Specification #ii

$$P_{od} = \pi_{od} + u_{od}$$

$$\pi_{od} = F(x'_{od}\beta)$$

$$P_{od} = F(x'_{od}\beta) + u_{od}$$

Non-linear GProbit model of flows

$$P_{od} = \Phi(x'_{od}\beta) + u_{od}$$

Can be linearized:

(*Gourrieroux 2000*, section 4.2):

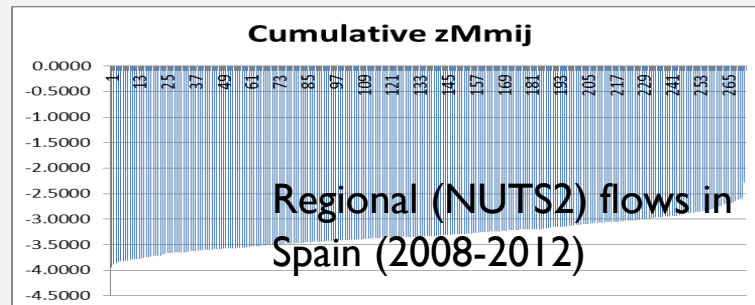
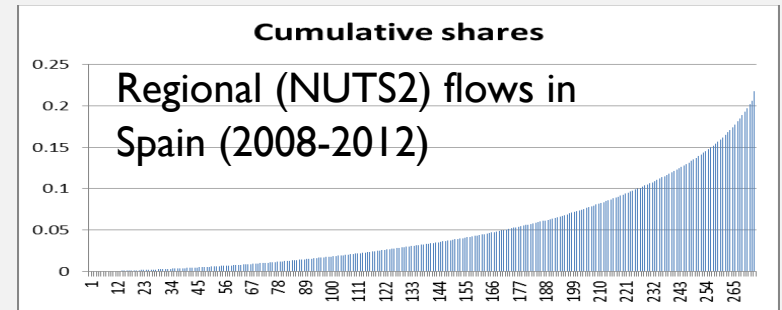
Slutsky's theorem on convergence in probability + Large number of group shares

$$Z_{od} = \Phi^{-1}(P_{od}) = \alpha \iota_N + X_d \beta_d + X_o \beta_o + \lambda D + \varepsilon_{od}$$

Linear function GProbit model of flows

Dependent variable:

Inverse of the cumulative standard normal distribution of  $P_{od}$



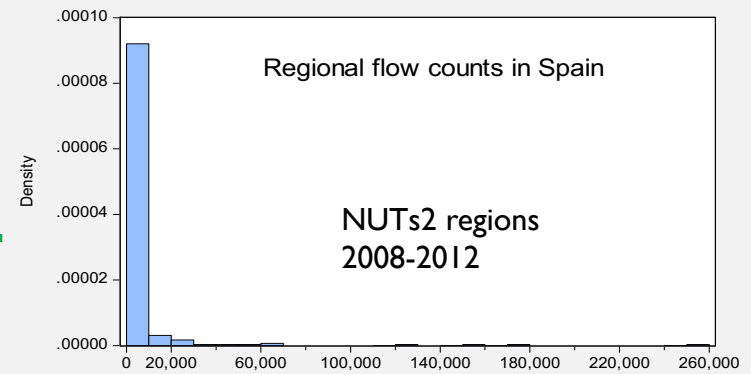
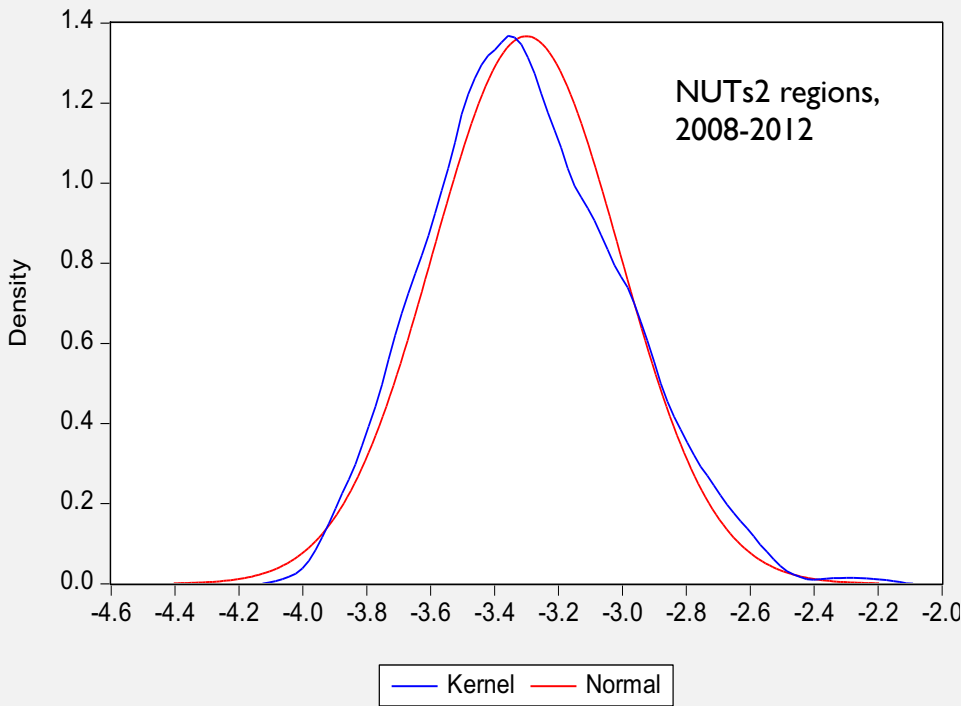
## II. GPROBIT: AN ALTERNATIVE

### II.2. Solutions for model problems #i

Problem	Spatial interaction model	Gprobit model for OD flows
Non-normality of count-data	Instead of counts, <b>log(counts)</b> (very frequent in the literature)	$y=z$ : inverse cumulative standard normal distribution of flow shares


Dependent variable ( $Z_{od}$ ): inverse cumulative standard **normal** distribution of flow shares.  
**Normality is assumed.**

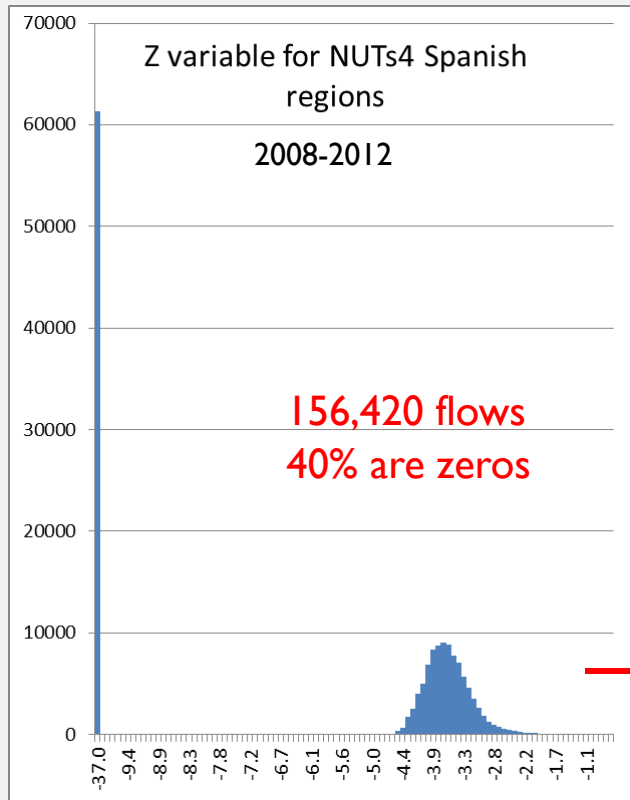
Z variable for regional flow shares in Spain



## II. GPROBIT: AN ALTERNATIVE

### II.2. Solutions for model problems #ii

Problem	Spatial interaction model	Gprobit model for OD flows
Zero flows	Instead of $\log(0)$ , $\log(1+0)$ (LeSage & Pace 2008)	z's domain is 0-1 (zero is included) 



**Zero** is theoretically part of the domain  $Z$  values, because it is part of the shares ( $P_{od}$ ):

$$Z = \Phi^{-1}(P_{od})$$

$$\text{Domain} = [0, 1]$$

In empirical apps. (STATA 2017), in order to linearize the model, the extreme values are:

$$Z = \Phi^{-1}(P_{od}) \rightarrow \text{Domain} = [10^{-323}, (1-2^{-53})].$$

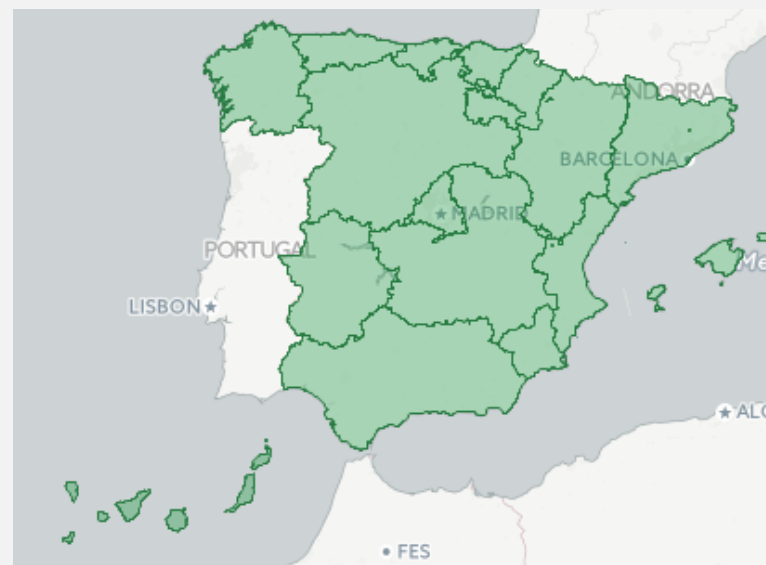
Hence, the values of the dependent variable  $Z$  range from  $-38.449394$  to  $8.2095362$ .

→ Zeros are possible values for  $Z$ , but always problematic when presented largely in a variable.



### III. EMPIRICAL ILLUSTRATION FOR MIGRATION INTERREGIONAL FLOWS ACROSS NUTS 2 IN SPAIN (2008 – 2012)

- We illustrate the performance of a GProbit model to estimate internal migration flows for the 17 NUTS 2 regions in Spain taken from the EVR register, INE.
- **Flows:** (emigrants from  $o$  to  $d$ ) / total  $o$ 's in/out-emigrants).
- We compare the performance and results of this model with the gravitational model using the conventional log transformation of flows for the dependent variable.





# III. EMPIRICAL ILLUSTRATION FOR MIGRATION INTERREGIONAL FLOWS ACROSS NUTS 2 IN SPAIN (2008 – 2012) #ii

Variable		Units	Source	Period
<i>Dependent variable:</i>				
<i>Mod</i>	Migrant flow (5-year sum)	Persons	Spanish National Statistics Office	2008-2012
<i>Independent variables:</i>				
<b>Income and quality of life</b>				
<i>pibpc</i>	GDP per capita	Euros	National Statistics Office (INE)	2003-2007
<i>incpc</i>	Household disposable income per capita	Euros	National Statistics Office (INE)	2003-2007
<i>wage</i>	Salaries and wages per capita	Euros	National Statistics Office (INE)	2003-2007
<i>act</i>	Activity rate growth	Percentage	National Statistics Office (INE)	2003-2007
<b>Labor and housing markets</b>				
<i>emp</i>	Population	Percentage	National Statistics Office (INE)	2003-2007
<i>unem</i>	Population	Percentage	National Statistics Office (INE)	2003-2007
<i>pviv</i>	Housing price	Euros	Ministry of Development of Spain	2003-2007
<i>delin</i>	People declaring having delinquency problems	Percentage	National Statistics Office (INE)	2003-2007
<b>Agglomeration economies</b>				
<i>Pop</i>	Population	Persons	National Statistics Office (INE)	2003-2007
<i>dens</i>	Population density	Persons per km <sup>2</sup>	National Statistics Office (INE)	2003-2007
<i>PPu</i>	Urban population share*	Percentage	National Statistics Office (INE) and self-elaboration	2003-2007
<i>pd3g</i>	Population aged 25-64 with university degree	Percentage	National Statistics Office (INE)	2003-2007
<i>rad</i>	R&D expenditure per capita	Thou. euros	National Statistics Office (INE)	2003-2007
<b>Natural endowments</b>				
<i>tmed</i>	Annual average temperature	Degrees	State Meteorological Agency	2003-2007
<i>tmax</i>	Annual maximum temperature	Degrees	State Meteorological Agency	2003-2007
<i>tmin</i>	Annual minimum temperature	Degrees	State Meteorological Agency	2003-2007
<i>sun</i>	Sun hours	Hours	State Meteorological Agency	2003-2007
<i>rain</i>	Atmospheric precipitation	Millimeters	State Meteorological Agency	2003-2007
<i>marit</i>	Length of coastline (destination)	Km	National Geographic Institute	2003-2007
<b>Distance:</b>				
<i>Dod</i>	Origin – destination distance	Km	Self-elaboration with GIS	-
<i>Tod</i>	Origin – destination travel time	Minutes	Self-elaboration with Google Maps	-

- . **Data** has been ordered according to the origin-centric scheme.
- . **Flows**: emigrants from o to d / total people of o who have changed their residence during this period (including intra-regional movements).
- . **X**: ‘push’ and ‘pull’ factors (ratio D/O values).
- . **D**: log-transformed distance between the capital cities.
- . In gravity model: log transformation of flows.



# GPROBIT: OLS

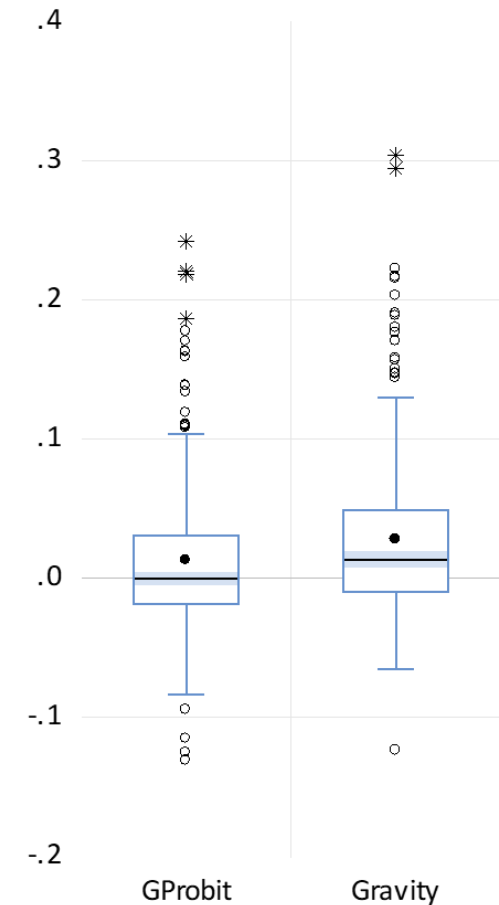
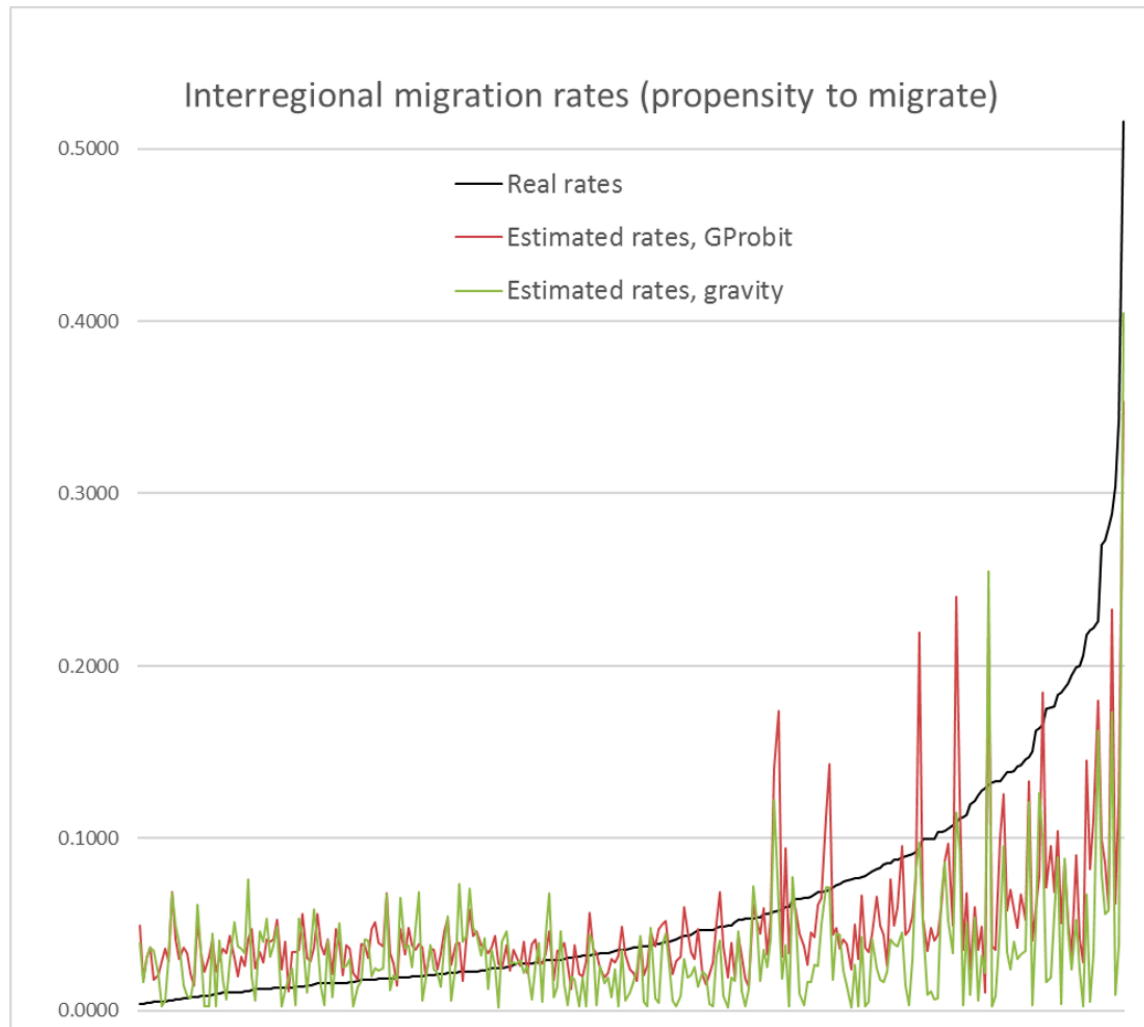
**Table 1:** Estimation results for the interregional migration models

Dependent variable	GProbit model	Gravity model	
	$Z_{od} = \Phi^{-1}(M_{od}/M_o)$	$\ln(M_{od})$	$\ln(M_{oo})$
	(1)	(2)	(3)
<i>Constant</i>	-1.820***	7.088***	13.044***
<i>Population D/O ratio</i>	0.036***	-	$0.4 \cdot e^{-7}$ ***
<i>Housing price D/O ratio</i>	-	-0.481**	-
<i>R&amp;D expenditure p.c. D/O ratio</i>	0.073***	0.137***	-
<i>Average altitude D/O ratio</i>	-0.083***	-0.245***	-
<i>Annual max. temperature D/O ratio</i>	-	-	-0.088*
<i>Atmospheric precipitation D/O ratio</i>	-0.081***	-	-
<i>O-D distance (log)</i>	-0.158***	-0.244**	-
Adj. R-squared	0.312	0.094	0.847
Prediction accuracy measures for the propensity to migrate: $\hat{P}_{od} = \hat{M}_{od} / \hat{M}_o$ :			
Bias indicator (RBIAS)	0.79	4.04	
Coefficient of variation (CV)	1.16	311.03	
Relative root mean sq. error (RRMSE)	0.16	0.35	

Note: A robust inference of the GProbit model estimators have been computed.



**Fig. 1.** Real, estimated and residual interregional flows, GProbit and gravity models



■ Difference btw. real and estimated rates



## IV. CONCLUSIONS

- Adjusted  $R^2$  takes a very low value, particularly for the gravity model estimation, which is in line with other previous analysis in the literature.
- Spanish interregional migration has long been resistant to traditional economic explanations., even to core variables of income and employment (Mulhern & Watson, 2009).
- The strong rigidity of the Spanish labor market, centrally controlled by the trade unions, and a very high national unemployment discourages internal migration (Bover & Velilla, 1999) and instead promotes migration to other countries.



## IV. CONCLUSIONS

- Only a few push & pull factors explain internal migration flows among Spanish regions.
- **Physical distance** in straight line from OD regional capital cities works better as a deterrence variable than travel time.
- Only **socioeconomic agglomeration** (population, house price and R&D investment), joint to **climate variables** explain internal flows among the Spanish regions.
- **Pending**: : analyze different types of migration flows by gender, age and nationality. Additionally, we also would like to apply this model approach to **other kind of flow data**.



# INE EXPERIMENTAL STATISTICS



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## Experimental statistics – Overview

### INTRODUCTION

Experimental statistics use new data sources and methods in an effort to better respond to our users' needs.

For example, for the first time Eurostat is estimating [price changes in the food supply chain](#), from farm to consumer. Another example is the use of Wikipedia as a new source to produce statistics on the [visits to UNESCO World Heritage Sites](#). This is to measure not only the popularity of the sites but also the public's 'cultural consumption'.



As these statistics have not reached full maturity in terms of harmonisation, coverage or methodology, they are always marked with a clearly visible [logo](#) and accompanied by detailed methodological notes.

On the webpage of each of the experimental statistics, you can use the 'Send us a message' function to give us your feedback on how to improve our experimental statistics!



# EUROSTAT EXPERIMENTAL STATISTICS

	TIME_PERIOD	REF_AREA	ROW_PI	AT	BE	BG	CY	CZ	DE	DK	EE
Y000	2010.0000	AT	CPA_N77	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_N78	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_N79	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_N80T82	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_O84	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_P85	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_Q86	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_Q87_88	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_R90T92	0.0000	0.0293	0.0004	0.0000	0.0351	0.1381	0.0011	0.0000
Y000	2010.0000	AT	CPA_R93	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_S94	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_S95	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_S96	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_T	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	CPA_U	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Y000	2010.0000	AT	P1_TR	0.0000	110.2927	41.0389	2.2487	21.8427	738.2287	4.1604	4.7000
Y000	2010.0000	BE	CPA_A01	4.6909	0.0000	0.1907	0.2686	1.7854	49.9638	0.2782	0.2000
Y000	2010.0000	BE	CPA_A02	0.0226	0.0000	0.0011	0.0001	0.0441	1.6632	0.0463	0.0000
Y000	2010.0000	BE	CPA_A03	0.3081	0.0000	0.0003	0.0128	0.0079	0.2229	0.0217	0.0000
Y000	2010.0000	BE	CPA_B	1.4868	0.0000	2.3000	0.0151	0.5998	70.0108	0.0202	0.0000
Y000	2010.0000	BE	CPA_C10T12	12.4209	0.0000	3.2608	3.1500	3.2888	88.3418	0.4066	1.1000
Y000	2010.0000	BE	CPA_C13T15	9.8250	0.0000	1.7666	0.6212	5.4963	31.9853	0.4266	1.3000
Y000	2010.0000	BE	CPA_C16	0.8437	0.0000	0.1078	0.0878	0.3249	10.3177	0.0560	0.0000
Y000	2010.0000	BE	CPA_C17	7.4544	0.0000	0.6479	0.4351	1.4874	21.7783	0.1386	0.0000
Y000	2010.0000	BE	CPA_C18	0.5698	0.0000	0.0006	0.0134	0.0330	0.1936	0.0000	0.0000

Figaro Tables of  
international &  
sectoral trade  
flows (in  
current prices).

Regional trade  
flows?

FIGARO\_ITTM\_MATRIX

+



**THANK YOU!**

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